## Bitcoin




1. Introduction

Commerce on the Internet has come to rely almost exclusively on financial institutions serving
as trusted third parties to process electronic payments. While the system works well enough for as trusted third parties to process electronic payments. While the system works well enough for
most transactions it still suffers from the inherent weakesses of the trust based model
Completely non-reversibile transactions are not really possible, since financial institututions cannot
 minimum practical transaction size and cutting orf the possibinity for small casual transactions,
and there is a broader ocst in the loss of aibity to make non-reversile payments for non-
reversible services. With the possibility of reversal, the need for trust spreads. Merchants must reversibe services. With the possibility of reversal, the need for trust spreads. Merchants must
be wary of their customers, hassing them for more inormation than they would otherwise ned.
A certain percentage of fraud is acceepted as unavoidable. These costs and payment uncertainties A certain percentage of fraud is accepted as unavoidable. These costs and payment uncertainties
can be voioded in person byusing yhysical currency but no mechanism exists to make payments
over a communications channel without a trusted party can be avoided in person by using physical currency, but
over a communications channel without a trusted party.

What is needed is an electronic payment system based on cryptographic proof instead of trust,
allowing any two willing partiesto to transact directly with each other without the need for a turused
this paty third party. Transactions that are computationally impractical to reverse would protect sellers
from fraud, and routine escrow mechanisms could easily be implemented to protect buyers. In
 ng group of attacker nodes.

## 2. Transactions

 We define an electronic coin as a chain of digital signatures. Each owner transfers the coin to thenexx thy digitalyly signing a hash of the errevious transaction and the pubbickeyof of the ent owner
and adding these to the end of the coin. A payee can verify the signatures to verify the chain of and adding these to the end of the coin. A payee can verify the signatures to verify the chain
ownership.


The problem of course is the payee can't verify that one of the owners did not double-spend the
coin. A common solution is to introduce a trusted central authority, or mint, that checks every coin. A common solution is to introduce a trusted central authority, or mint, that checks every
transaction for double spending. After each transaction, the coin must be erturned to the mint to
issue anew issue a new coin, and only coins issued directly from the mint are trusted not to be double-spent.
The problem with this solutuon is that the fate of the entire money system depends on the
company running the mint, with every transaction having to go through them, just ike a bank.

We need a way for the payee to know that the previous owners did not sign any earlier
transactions. For our purposes, the earliest transaction is the one that counts, so we don't care
 decided which arrived first. To accomplish this without a trusted party, transactions must be
publicly announced, and we eed system for participants to agree on a single history of the
order in which they were received. The payee needs proof that at the time of each transsaction, eeived. The payee need

## 3. Timestamp Server

The solution we propose begins with a timestamp server. A timestamp server works by taking a
hash of a block of items to be timestamped and widely publishing the hash, such as in hewspaper or Usenet postw.. The timestamp proves that the data must have existed at the time
bviously, in order to get into the hash. Each timestamp includes the previos timest hash, forming a chain, with each additional timestamp reinforcing the ones before it.

| $\xrightarrow{\text { Hash }}$ | $\longrightarrow$ Hash |  |  |
| :---: | :---: | :---: | :---: |
| Block | Block |  |  |
| Hem tem | Hem | tem | $\cdots$ |

4. Proof-of-Work

To implement a distributed timestamp server on a peer-to-peer basis, we will need to use a proof
of-work system similar to Adam Back's Hashcash, rather than newspaper or Usenet posts. The proof-of-work involves scanning for a value that when hashed, such as with SHA-255, the hash
begeins with a number of zero
zerso . The average work required is exponential in the number of For our timestamp network, we implement the proof-of-work by incrementing a nonce in the
block until a value is iswund that gives the block's hash the eruired zero bits. Once the cev effort
has been expended to make it satisfy the proof-of-work, the block cannot be changed without has been expenced to make it satisfy the proof-or-work, the block cannot be changed without
redoing the work. As alaet blocks are chained after it, the work to change the block would include
redoing all the blocks after it.


The proof-of-work also solves the problem of determining representation in majority decision
making. If the majority were based on one-IP-address-one-vote, it could be subverted by anyone able to allocate many IPs. Proof-of-work is essentially one-CPU-one-vote. The majority decision i
eepresented by the longest chain, which has the greatest proof-of-work effort invested in it. If represented by the longest chain, which has the greatest proof-of-work effirr tinvested in it. If a
majority of CPU power is controlled by honest nodes, the honest chain will grow the fastest and
outpace any comenting chains To modify outpace any competing chains. To modify a past block, an attacker would have to redo the proof-
of-work of the block and all loock atfer it and then catch up with and surpass the work of the
howest nodes. We will show later that the probability of a slower attacker catching up dimininhes
exponentially as subsequent locks are added. exponentially as subsequent blocks are added.

To compensate for increasing hardware speed and varying interest in running nodes over time,
the profof-owork dificulty id detemined by a moving verage targeting an average number of
blocks per hour If theyre generated too fast, the difficulty increases.
5. Network
$\qquad$

1. New transactions are broadcast to all nodes.
2. 

Each node collects new transactions into a block

 Nodes accept the block only if all transactions in it are valid and not already spent.
Nodes express their aceetanco of he block byorking on creating the next block in
the chain, using the hash of the accepted block as the previous hash.

Nodes always consider the longest chain to be the correct one and will keep working on extending
t. If two nodes broadcast different versions of the next block simultaneously, some nodes maa eeceive one or the other first. In that case, they work on the first one they received, but save the
other branch the other branch in case it becomes longer. The tie will be broken when the next proof-of-work
found and one banch becomes longer, the nodes that were working on the other branch will the
switch to the longer one.


## 6. Incentive

By convention, the first transaction in a block is a special transaction that starts a new coin
owned by the creator of the block. This adds an incentive for nodes to support the network, and provides a way to initially distribute coins into circulation, since there is no central authority to issue them. The steady addition of a constant of amount of new coins is analogous to gold miners
expending resources to add gold to circulation. In our case, it is CPU time and electricity that is
expended.

The incentive can also be funded with transaction fees. If the output value of a transaction is less
than its input value, the difference is a transaction fee that is added to the incentive value of the than its input value, the difference is a transaction fee that is added to the incentive value of the
bock containing the rransaction. Once a predeetrmined number of coins have entered circulation,
the incentive can transition entirely to transaction fees and be completely inflotion free

The incentive mey help encourage nodes to stay honest. If a greedy attacker is able to assemble
more CPD power than all the honest nodes, he would have to choose between using it to defraud people by stealing back his payments, or using it to generate new coins. He ought to find it more
profitable to play by the rules. such rules that faour him with more new coiss than everyone
else combined, than to undermine the system and the validity of his own wealth.
7. Reclaiming Disk Space

Once the latest transaction in a coin is buried under enough blocks, the spent transactions before
it can be discarded to save disk space. To facilitate this without breaking the block's hash,
transaction transactions are hashed in a Merkle Tree en, with only the root included in the block's hash. Old
blocks san then be compacted by stubbing off branches of the tree. The interior hashes do not blocks can then be
need to be stored.


A block header with no transactions would be about 80 bytes. If we suppose blocks are generated
every 10 minutes, 8 bytes $* * * * * * 365=4.2 \mathrm{MB}$ per year. . With computer systems typically

8. Simplified Payment Verification

It is possible to verify payments without running a full network node. A user only needs to keep
a copy of the block headers of the longest proof-of-work chain which he can se a copy of the block headers of the longest proof-of-work chain, which he can get by querying
network nodes until hes convinced he has he olvest chain, and obtain the Merkle branch
linking the transaction to the block it's timestamped in. He can theck the transaction for himself, linking the transaction to the block its titestamped in. He cant t heck the transaction for himself,
but by linking it to a place in the chain, he can see that a network node has accepted it, and
blocks added after it further confirm the network has accepted it.


As such, the verification is reliable as long as honest nodes control the network, but is more
vulnerable if the network is overpowered by an attacker. While network nodes can verify transactions for themselves. the simperified method can be fooled by an ark notaceses can verinity
transactions for as long as the attacker can continue to overpower the network. One strateat to transactions for as long as the attacker can continue to overpower the network. One strategy to
protect against this would be to accept alarts from nettork nodes when they detect an invalid
block, prompting the user's software to download the full block and alerted transactions to

9. Combining and Splitting Value

Although it would be possible to handle coins individually, it would be unwieldy to make a
separate transaction for every cent in a a transfer. To allow value to be split a nd combine separate transaction for every cent in a transfer. To allow value to be split and combined,
transactions contain multiple inputs and outuputs. Normaly there will be either a single input
from a larger previous transaction or multiple inputs combining smaller amounts, and at most transactions contain multiple inputs and outputs. Normally there will be ee either a single input
from a larger previous tansaction or multipl inputs combining smalle amouns. and at most
two outputs: one for the payment, and one returning the change, if any, back to the sender.


It should be noted that fan-out, where a transaction depends on several transactions, and those
transactions depend on many more, is not a problem here. There is never the need to extract a transactions depend on many more, is not a prob
complete standalone copy of a transaction's history.

## 10. Privacy

The traditional banking model achieves a level of privacy by limiting access to information to the
parties involved and the trusted third party. The necessity to announce all transactions publicly parties involved and the trusted third party. The necessity to announce all transactions publicly
precludes this method, but privacy can still be maintained by breaking the flow of information in prectudes slace: by keeping public keys suonymous. The public can see that someone is sending
anothe paran
an amount to someone else, but without information inking the transaction to anyone. This is
similar to the level of information released by stock exchanges, where the time and size of similar to the level of information released by stock exchanges, where the time an
individual trades, the "tape", is made public, but without telling who the parties were.


[^0]11. Calculations

We consider the scenario of an attacker trying to generate an alternate chain faster than the
honest chain. Even if this is accomplished, it does not throw the system open to arbitrary changes, such as creating value out of thin air or taking money that never belonged to the attacker. Nodes are not going to accept an invalid transaction as payment, and honest nodes will never accept a
block containing them An attacker can only try to change one of his own transactions to take
back money he recently spent.

The race between the honest chain and an attacker chain can be characterized as a Binomial
Random Walk. The success event is the honest chain being extended by one block inereasimits Random Walk. The success event is the honest chain being extended by one block, increasing its
lead by +1 , and the failure event is the attacker's chain being extended by one block, reducing
the gap by -

The probability of an attacker catching up from a given deficit is analogous to a Gambler's Ruin
problem. Suppose a a gambler with unlimited credit starts at a deficit and plays potentially an infinite number of trials to try to reach breakeven. We can calculate the probability he ever
reaches breakeven, or that an attacker ever catches up with the honest chain, as follows.:
$p=$ probability an honest node finds the next block
$q=$ probability the attacker finds the next block
$q_{z}=$ probability the attacker will ever catch up from $z$ blocks behind
$q_{z}=\left\{\begin{array}{cl}1 & \text { if } p \leq q \\ (q / p)^{z} & \text { if } p>q\end{array}\right\}$
Given our assumption that $p>q$, the probability drops exponentially as the number of blocks the
attacker has to catch up with increases. With the odds against him, if he doesnt take
lunge forward early on, his chances become vanishingly small as he falls further behind.
We now consider how long the recipient of a new transaction needs to wait before being
sufficiently certain the sender can't change the transaction. We assume the sender is an attacker who wants to make the recipient believe he paid him for a while, then switch it to pay back to
himself atter some time has passed. The receiver will be alerted when that happens, but the
sender hopes it will be too late.

The receiver generates a new key pair and gives the public key to the sender shortly before signing.
This rpeentst he sender from preparing a chain of blocks ahead of time by working on it
continuously until he is lucky enough to get far enough head then executing the transaction at continuously until he is lucky enough to get far enough ahead, then executing the transaction at
that moment. Once the transaction is sent, the dishonest sender starts working in secret on a parallel chain containing an alternate version of hish transtaction.

The recipient waits until the transaction has been added to a block and $z$ blocks have been linked
after it. He doesn't know the exact mount of progress the attacker has made but assuming the

$\lambda=z \frac{q}{p}$
To get the probability the attacker could still catch up now, we multiply the Poisson density for
each amount of progress he could have made by the probability he could catch up from that point:
$\sum_{k=0}^{\infty} \frac{\lambda^{k} e^{-\lambda}}{k!} \cdot\left\{\begin{array}{cc}(q / p)^{(z-k)} & \text { if } k \leq z \\ 1 & \text { if } k>z\end{array}\right\}$
Rearranging to avoid summing the infinite tail of the distribution...
$1-\sum_{k=0}^{z} \frac{\lambda^{k} e^{-\lambda}}{k!}\left\{1-(q / p)^{(z-k)}\right\}$
Converting to C code..




$\qquad$

$\qquad$
12. Conclusion

We have proposed a system for electronic transactions without relying on trust. We started with
the usual framework of coins made from digital signatures, which provides strong control of the usual framework of coins made from digital signatures, which provides strong control of
onnershi, but is incomplete without a way to prevent double-spending. To solve this, we
proposed a peer-to-per network using proof-ofwrk to tecord

 While they were gone. They vote with their CPU power, expressing their acceptance of valid blocks
by working on extenidig them and rejecting invalid blocks by refusing to work on them. Any
needed rules and incentives can be enforced with this consensus mechanism.

## References




[^0]:    As an additional firewall, a new key pair should be used for each transsaction to keep them from
    being linked to a common owner. Some linking is still unavoidable with multi-input transactions being linked to a common owner. Some linking is still unavoidable with multi-input transactions,
    which necessarily reveal that their inputs were owned by the same owner. The risk is that if the
    owner of a key is revealed, linking could reveal other transactions that belonged to the same

